

Middle East Technical University  
Department of Mathematics

## GENERAL SEMINAR

### “Guessing and Sequential Decoding”

**Abstract:** The guessing problem is the following: Let  $(X, Y) \sim P_{X,Y}$  be a pair of discrete random variables with  $X$  taking one of  $M$  possible values. Suppose the value of  $X$  is to be determined, given the value of  $Y$ , by asking questions of the form ‘Is  $X$  equal to  $x$ ?’ until the answer is ‘Yes.’ Let  $G(x|y)$  denote the number of guesses in any such guessing scheme when  $X = x$ ,  $Y = y$ . We prove that the moments of the guessing effort satisfy the inequality  $E[G(X|Y)^\rho] \geq (1 + \ln M)^{-\rho} \sum_y [\sum_x P_{X,Y}(x, y)^{\frac{1}{1+\rho}}]^{1+\rho}$  for any  $\rho \geq 0$ .

We apply this inequality to the estimation of the computational complexity in sequential decoding, which is a decoding algorithm for error correction codes. For this, we regard  $X$  as the input,  $Y$  as the output of a communication channel. Given  $Y$ , the sequential decoding algorithm works essentially by guessing  $X$ , one value at a time, until the guess is correct. Thus, the computational complexity of sequential decoding, which is a random variable, is given by a guessing function  $G(X|Y)$  that is defined by the order in which nodes in the tree code are hypothesized by the decoder. This observation, combined with the above lower bound on moments of  $G(X|Y)$ , yields lower bounds on moments of computation for sequential decoding, and furnishes a simple method for determining the *computational cutoff rate* for single-user and multi-access channels.

**Speaker: Erdal Arıkan (Bilkent University)**

Date: 11 May 2006 Thursday  
Place: G. Ikeda Seminar Room  
Time: 15:40